

- Need to rewrite the entire program if more houses were added.
- What we really need is lists...


## Support for lists in Prolog

- Notated with square brackets [1, 2, 3, 4].
- The empty list is [ ] .
- List pattern matching is $[\mathrm{H} \mid \mathrm{T}$ ], where H is a list element and $T$ is a list.
- Can also match [1,2,3|T].


## Finding the last element of the list

In [1]:

```
last([H],H).
last([_ | T], V) :- last(T, V).
```

Added 2 clauses(s).

In [2]:
?- last([1,2],X).
$X=2$

## Tracing the example by hand

last([1,2],X).

## Tracing the example in SWI-Prolog

last ([1,2],X)

## Quiz

What happens if I ask for last([ ], X) ?

1. pattern match exception
2. Prolog says false.
3. Prolog says true, $X=[]$.
4. Prolog says true, $X=$ ???.

## Quiz

What happens if I ask for last([ ], X) ?

1. pattern match exception
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4. Prolog says true, $X=$ ???.

## Arithmetic

- How do we compute the length of the list?
- We need support for arithmetic.
- Arithmetic is quite natural in imperative and functional paradigms.
- Since computation is deduction in logic programming, arithmetic is quite special.


## Arithmetic equality != Unification

$=$ operator is used up by unification.

In [3]:
? $-\mathrm{A}=1+2$.
$A=+(1,2)$.

In [4]:
? $-1+2=3$.
false.

In [5]:
?- $\mathrm{A}=$ money+power.
$A=+(m o n e y$, power $)$.

## Use the is operator

The "is" operator tells prolog to evaluate the righthand expression numerically and unify with the left.

In [6]:
?- $X$ is $1, A$ is $X+2, X$ is 2.
false.

In [7]:
?- A is money+power.
ERROR: Caused by: ' A is money+power'. Returned: 'error(type_error(ev aluable, /(power, 0)), context(:(system, /(is, 2)), _1768))'.

## Restriction on is operator

The RHS must be a ground term (no variables).

In [8]:
? - $A$ is $B+2$.
ERROR: Caused by: ' A is B+2'. Returned: 'error(instantiation_error, context(: (system, /(is, 2)), _1914))'.

In [9]:
?- 3 is $\mathrm{B}+2$.
ERROR: Caused by: ' 3 is $\mathrm{B}+2$ '. Returned: 'error(instantiation_error, context(: (system, /(is, 2)), _2048))'.

## Quiz

What is the result of A is * $(3,+(1,2))$ ?

1. Error
2. 9
3. 8
4. 6

## Quiz

What is the result of A is * $(3,+(1,2))$ ?

1. Error
2. $9 \sqrt{ }$
3. 8
4. 6

## Arithmetic

There is support for $+, *, /,<,=<,>,>=$, etc.

In [10]:
?-20 / 20 .
ERROR: Caused by: ' 20 / 20'. Returned: 'error(type_error(lambda_fre e, 20), _2146)'.

## List Sum

Compute the sum of the list. This is the example we saw in the first Prolog lecture.

## In [11]:

```
sum([],0).
sum([H | T], N) :- sum(T,M), N is M+H.
```

Added 2 clauses(s).

In [12]:
?- $\operatorname{sum}([1,2,3], X)$.
$x=6$.

In [13]:
?- $\operatorname{sum}(X, 3)$.
ERROR: Caused by: ' sum(X,3)'. Returned: 'error(instantiation_error, context(: (system, /(is, 2)), _2280))'.

## Length of list

In [14]:
$\operatorname{len}([], 0)$.
$\operatorname{len}\left(\left[\_\mid T\right], N\right):-\operatorname{len}(T, M), N$ is $M+1$.
Added 2 clauses(s).

In [15]:
?- len([1,2,3],X).
$\mathrm{X}=3$.

## Last call optimisation

- len uses $\mathrm{O}(\mathrm{N})$ stack space.


## Trace len by hand

?- $\operatorname{len}([1,2], X)$

## Tail recursive length

In [16]:

```
len2([],Acc,Acc).
len2([H|T],Acc,N) :- M is Acc+1, len2(T,M,N).
```

Added 2 clauses(s).

In [17]:
?- len2 ([1, 2],0, X).
$\mathrm{X}=2$

## Trace len2 by hand.

```
?- len2([1,2],0,X).
```


## Predicate Overloading

In [18]:
$\operatorname{len} 2(L, X):-\operatorname{len} 2(L, 0, X)$.
Added 1 clauses(s).

In [19]:
?- len2 ([1,2,3],X).
$X=3$.

## Last Call Optimisation

- This technique is applied by the prolog interpreter
- The last clause of the rule is executed as a branch and not a call
- We can only do this if the rule is determinate up to that point
- No further choices for the rule
- Relates to choice points (to be seen).


## List append

In [20]:

```
append([],Q,Q).
append([H | P], Q, [H | R]) :- append(P, Q, R).
Added 2 clauses(s).
In [21]:
?- append([1,2],X,[1,2,3,4]).
X = [ 3, 4 ] .
```


## Prefix and Suffix

Prefix and Suffix of list can be defined using append.

In [22]:

```
prefix(X,Z) :- append(X,Y,Z).
suffix(Y,Z) :- append(X,Y,Z).
```

Added 2 clauses (s).

## Prefix and Suffix

In [23]:
?- prefix(X,[1,2,3]).
$\mathrm{X}=[\mathrm{l}$;
$\mathrm{X}=\left[\begin{array}{ll}\mathrm{l} & 1\end{array}\right]$
$\mathrm{X}=[1,2]$;
$X=[1,2,3]$.

In [24]:
?- suffix(X,[1,2,3]).
$\mathrm{X}=[1,2,3]$;
$\mathrm{X}=[2,3]$;
$\mathrm{X}=\left[\begin{array}{ll}{[ } & 3\end{array}\right]$;
$\mathrm{X}=\left[\begin{array}{l}\mathrm{l}\end{array}\right.$.

## Backtracking

The way prolog fetches multiple results for the given query is through Backtracking.

## Trace prefix by hand

```
?- prefix([1,2],X).
```


## Choice Points

- Choice points are locations in the search where we could take another option.
- If there are no choice points left then Prolog doesn't offer the user any more answers


## Quiz

What is the first result of query $\operatorname{len}(\mathrm{A}, 2)$ ?

1. Error due uninstantiated arithmetic expression.
2. $\mathrm{A}=[,$,
3. Query runs forever
4. Error due to invalid arguments

## Quiz

What is the first result of query $\operatorname{len}(\mathrm{A}, 2)$ ?

1. Error due uninstantiated arithmetic expression.
2. $A=[,$,
3. Query runs forever
4. Error due to invalid arguments

## Trace len by hand

?- len(A,2)

## Quiz

What is the second result of query len(A,2) ?

1. Error due uninstantiated arithmetic expression.
2. $\mathrm{A}=[,, \mathrm{]}$
3. Query runs forever
4. Error due to invalid arguments

## Quiz

What is the second result of query len $(\mathrm{A}, 2)$ ?

1. Error due uninstantiated arithmetic expression.
2. $\mathrm{A}=[,$,
3. Query runs forever $\checkmark$
4. Error due to invalid arguments

## Trace len by hand

?- len(A, 2)

Limiting the number of results

In [25]:
?- $\operatorname{len}(A, 2)\{1\}$.
$A=\left[\quad 2380, ~ \_2386\right.$ ] .
Fin.

